

Quadratic inequalities

A LEVEL LINKS

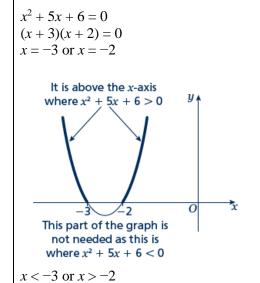
Scheme of work: 1d. Inequalities – linear and quadratic (including graphical solutions)

Key points

- First replace the inequality sign by = and solve the quadratic equation.
- Sketch the graph of the quadratic function.
- Use the graph to find the values which satisfy the quadratic inequality.

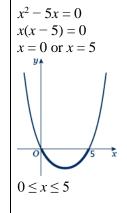
Examples

Example 1 Find the set of values of x which satisfy $x^2 + 5x + 6 > 0$



- 1 Solve the quadratic equation by factorising.
- 2 Sketch the graph of y = (x + 3)(x + 2)
- 3 Identify on the graph where $x^2 + 5x + 6 > 0$, i.e. where y > 0
- Write down the values which satisfy the inequality $x^2 + 5x + 6 > 0$

Example 2 Find the set of values of x which satisfy $x^2 - 5x \le 0$



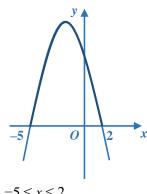
- 1 Solve the quadratic equation by factorising.
- 2 Sketch the graph of y = x(x 5)
- 3 Identify on the graph where $x^2 5x \le 0$, i.e. where $y \le 0$
- Write down the values which satisfy the inequality $x^2 5x \le 0$





Example 3 Find the set of values of x which satisfy $-x^2 - 3x + 10 \ge 0$

$$-x^{2} - 3x + 10 = 0$$
$$(-x + 2)(x + 5) = 0$$
$$x = 2 \text{ or } x = -5$$



- 1 Solve the quadratic equation by factorising.
- 2 Sketch the graph of y = (-x + 2)(x + 5) = 0
- 3 Identify on the graph where $-x^2 3x + 10 \ge 0$, i.e. where $y \ge 0$
- 3 Write down the values which satisfy the inequality $-x^2 3x + 10 \ge 0$

Practice

- 1 Find the set of values of x for which $(x + 7)(x 4) \le 0$
- 2 Find the set of values of x for which $x^2 4x 12 \ge 0$
- 3 Find the set of values of x for which $2x^2 7x + 3 < 0$
- 4 Find the set of values of x for which $4x^2 + 4x 3 > 0$
- 5 Find the set of values of x for which $12 + x x^2 \ge 0$

Extend

Find the set of values which satisfy the following inequalities.

- 6 $x^2 + x \le 6$
- 7 x(2x-9) < -10
- 8 $6x^2 \ge 15 + x$